

(2)

(6) If

$$S_{F_{\alpha\beta}}(x-y) = (i \not{\partial} + m) D_F(x-y)$$

Show that:

$$S_{F_{\alpha\beta}}(x-y) = \frac{1}{(2\pi)^4} \int d^4 p e^{-i p(x-y)} \left(\frac{i}{\not{p} - m} \right)_{\alpha\beta}$$

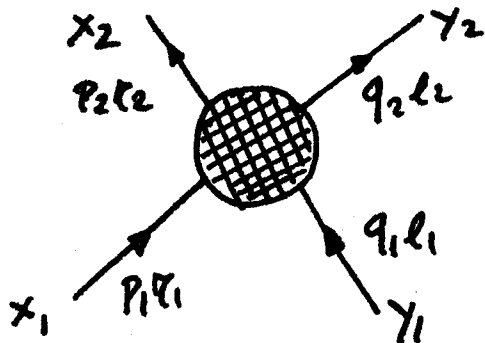
(5)

(7) Show that:

$$b_{1\alpha}(\vec{p}) = \frac{1}{(2\pi)^{3/2}} \sqrt{\frac{M}{E}} \int d^3 x \tilde{U}_\alpha(\vec{p}) \gamma^0 \psi_{1\alpha}(x) e^{i p x}$$

(10)

(8) Consider the 4 fermion process where $p_1 + q_1 \rightarrow p_2 + q_2$



4 fermions of 4-momenta p_1, p_2, q_1, q_2 and spin l_1, l_2, l_1, l_2

Show that the amplitude for this process is: $\langle p_2 l_2 q_2 l_2 | p_1 l_1 q_1 l_1 \rangle_{in}^{out}$

$$= \frac{-i}{(2\pi)^{3/2}} \sqrt{\frac{M}{E_{p_1}}} \int d^4 x e^{-i p_1 x} \langle p_2 l_2 q_2 l_2 | \tilde{\Psi}(x) | q_1 l_1 \rangle (-i \not{\partial} - m) U_\alpha(\vec{p}_1)$$

$$= \frac{(i)}{\sqrt{(2\pi)^3}} \frac{(-i)}{\sqrt{(2\pi)^3}} \frac{(i)}{\sqrt{(2\pi)^3}} \frac{(-i)}{\sqrt{(2\pi)^3}} \sqrt{\frac{M}{E_{p_1}}} \sqrt{\frac{M}{E_{p_2}}} \sqrt{\frac{M}{E_{q_1}}} \sqrt{\frac{M}{E_{q_2}}} \times$$

$$\int d^4 x_1 \int d^4 x_2 \int d^4 y_1 \int d^4 y_2 e^{-i(p_1 x_1 + q_1 y_1 - p_2 x_2 - q_2 y_2)} \times$$

$$\begin{aligned} & [\bar{U}(r_2 p_2) (\not{\delta} \cdot p_2 - m)]_\alpha [\bar{U}(q_2 l_2) (\not{\delta} \cdot q_2 - m)]_\beta \\ & \langle 0 | T \{ \psi_\alpha(x_2) \psi_\beta(y_2) \tilde{\Psi}_\delta(x_1) \tilde{\Psi}_\delta(y_1) e^{-i \int M \bar{\Psi} d^4 u} \} | 0 \rangle \times \\ & [(\not{\delta} \cdot p_1 - m) U(r_1 p_1)]_\delta [(\not{\delta} \cdot q_1 - m) U(l_1 q_1)]_\delta \end{aligned}$$

What process do you get from the e^2 contribution ?